

* Permutation *

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means of permutation is "arrangement"

we are giving a exam subject M, R, E

M, R, E \rightarrow total \rightarrow 3

RME MRE EMR
REM MER ERM \rightarrow total way 6

or $3! \rightarrow 3 \times 2 \rightarrow \underline{6}$

M R E

$\underline{3} \quad \underline{2} \quad \underline{1} \Rightarrow 3 \times 2 \times 1 \rightarrow \underline{6}$
Choice choice choice

ex! \rightarrow 1, 2, 3, 4 \rightarrow two digit no. (no repetition)

$\begin{array}{c} 4 \quad 3 \\ \underline{\quad} \quad \underline{\quad} \end{array} \leftarrow \begin{array}{c} 1 \\ \leftarrow \end{array} \begin{array}{c} 4-1 \rightarrow 3 \end{array}$
choice choice $\Rightarrow 4 \times 3 = \underline{12}$

ex! 1, 2, 3, 6, 7, 8, 9 \rightarrow four digit no.

i) can not repeat

ii) can repeat

ex! \rightarrow i) four digit total no \rightarrow 7

$\underline{7} \times \underline{6} \times \underline{5} \times \underline{4} \rightarrow \underline{840}$ ways

ii)

$\underline{7} \times \underline{7} \times \underline{7} \times \underline{7} \rightarrow \underline{2401}$ ways

Q1) 1, 2, 3, 6, 7, 8, 0 → total no → 7

find no. of ways. four digit

- i) not repeat
- ii) can repeat

solⁿ! → i) 6 × 6 × 5 × 4 → 720 way

total → 7, but never consider 0 at first place then total no → 6

now for next 0 will consider total 7
1 → choice, now left with 6.

ii)

← 6 × 7 × 7 × 7 ⇒ 2058
(42) (49)

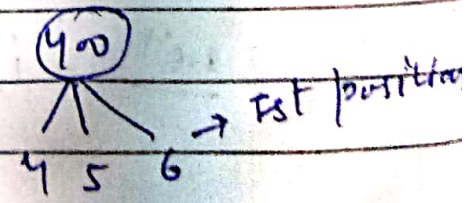
$$42(80-1) \\ 2100 - 42 \\ \underline{2058}$$

0's not consider at first place

now total no. 187

Q 2, 3, 4, 0, 5, 6 → 3 digit no greater than 400. (can not repeat)

3 × 5 × 4 → (60)
Ans



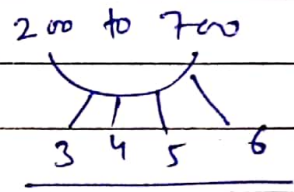
total no. → 6

Q1 → 1, 4, 3, 0, 5, 6 → 3 digit no. b/w 200 to 700.

imp point →

b/w → 201 - 699
from → 200 - 700

$\underline{4} \times \underline{5} \times \underline{4} \Rightarrow \textcircled{80} \text{ Ans}$



total no → 6 - 1 → 5

Q2 → 1, 2, 3, 4, 5, 6 → four digit no which is divisible by 5.

Sol → 1, 2, 3, 4, 5, 6

start from right

$\underline{5} \times \underline{4} \times \underline{3} \times \frac{\textcircled{0/5}}{1} \Rightarrow \textcircled{60} \text{ Ans}$

total → 6 - 1 → 5

Q3 → 0, 1, 2, 3, 4, 5, 6 → four digit which is divisible by 5.

Sol → when 0 present give uncertainty. use both case

$\underline{6} \times \underline{5} \times \underline{4} \times \underline{0}$

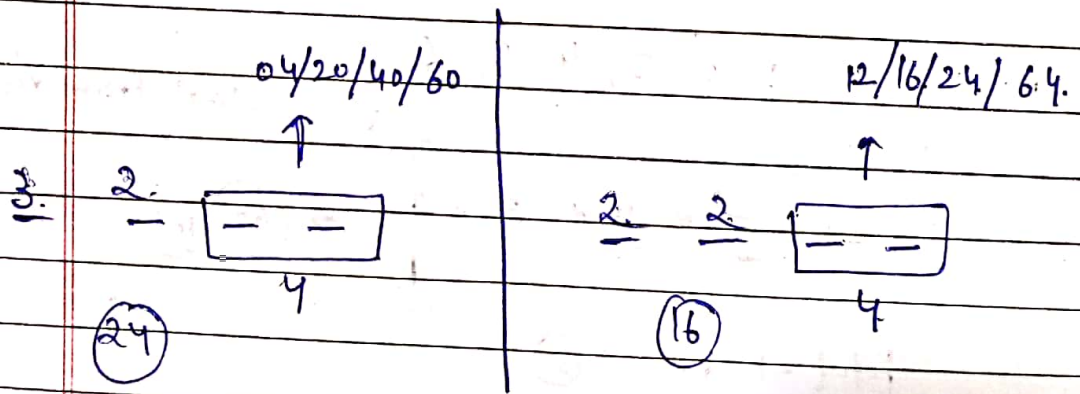
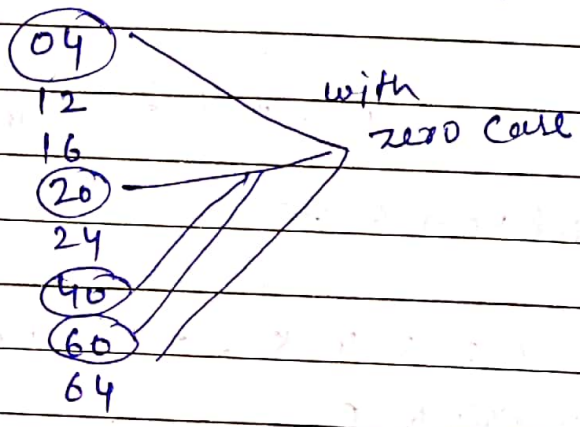
$\underline{5} \times \underline{5} \times \underline{4} \times \underline{5} \Rightarrow \textcircled{100}$

total → 7 - 1 = 6
total way
120 + 100
 $\boxed{220} \text{ Ans}$

total → 6, but 0 must place first
→ then 6 - 1 → 5 choice
now include 0 for next position.
5 → choice

Q! → 2, 1, 0, 4, 6 → four digit no.
which is divisible by 4. (4)

Sol for last two digit must divisible by 4.

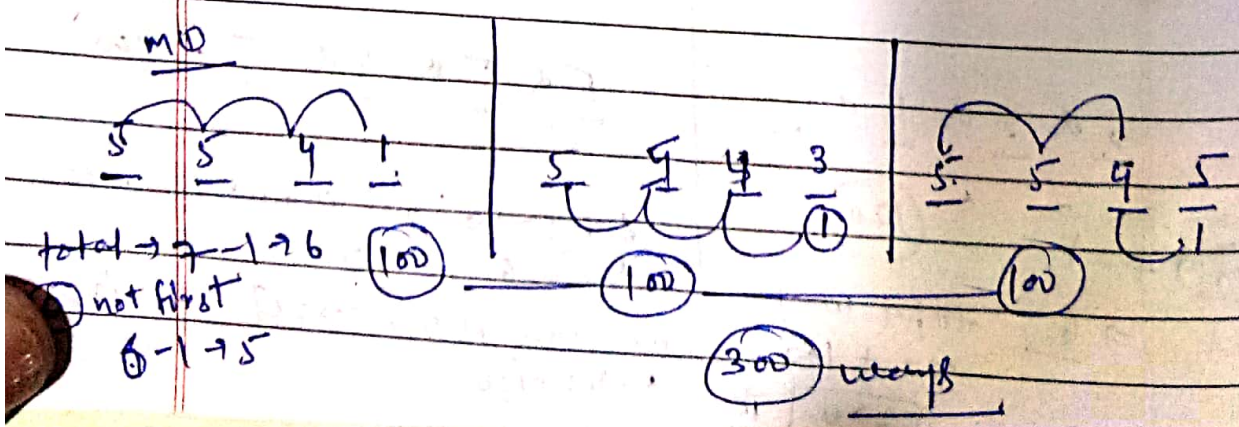


$24 + 16 \rightarrow 40$ ways Ans

Q! → make four digit odd no.

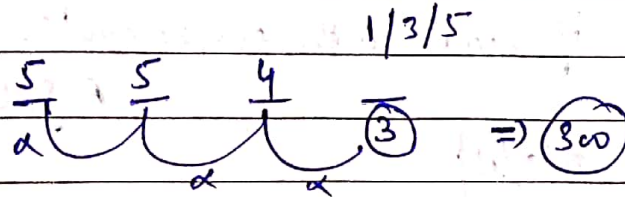
0, 1, 2, 3, 4, 5, 6

Sol for odd no. last digit → 1, 3, 5



total → 7 → 6
not first
6 → 5

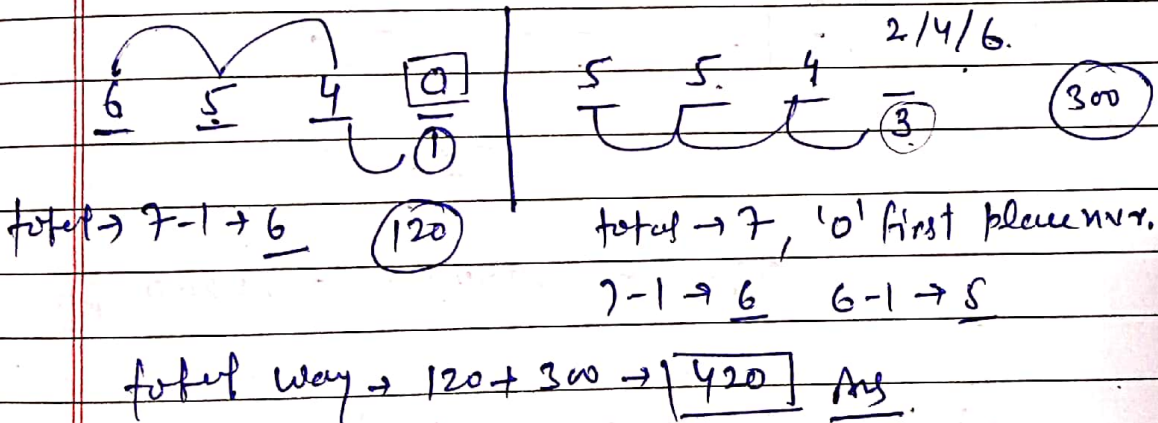
Q2 ! \rightarrow



Q! \Rightarrow make four digit even no.

0, 1, 2, 3, 4, 5, 6

even \rightarrow 0/2/4/6

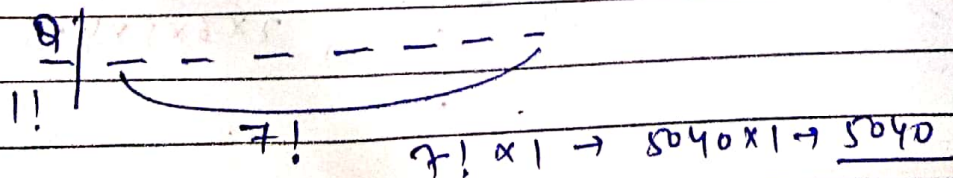


Q! \rightarrow In how many way we can arrange

i) EQUATION

way $\rightarrow 8! \rightarrow 8 \times 7! \rightarrow 8 \times 5040$

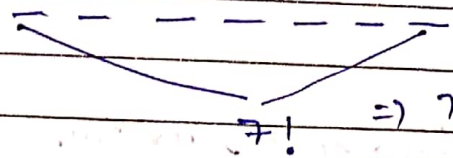
ii) if start letter Q.



iii) if start with consonants.

EQUATION

Q/T/N/
3



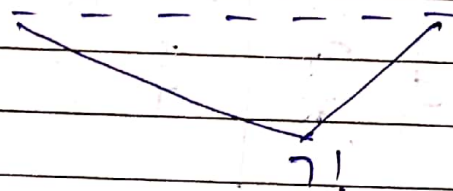
$\Rightarrow 7! \times 3$

$\Rightarrow 5040 \times 3 \Rightarrow \underline{15120}$ Ans

iv) if start with vowel

EQUATION

E/U/A/I/O/
5



$7! \times 5 \rightarrow 5040 \times 5 \Rightarrow \underline{25200}$ Ans

v) if start with consonants & end with vowel.

Q/T/N/
3

6!

E/U/A/I/O/
5

$\Rightarrow 6! \times 3 \times 5 \rightarrow 720 \times 15 \Rightarrow \underline{10800}$ Ans

Q! \rightarrow arrange BANKING

$\Rightarrow \frac{7!}{2!} \Rightarrow 7 \times 6 \times 5 \times 4 \times 3 \rightarrow \underline{2520}$

Answers ...

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Q1 → ASSASSINATION

all 's' are together.

total s → 4 (make 1)

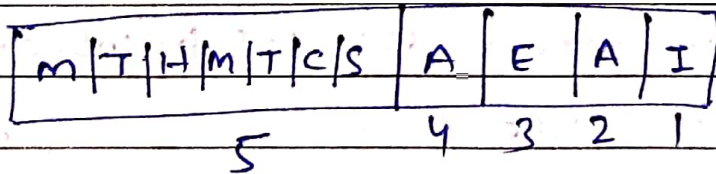
$$\underline{A} \underline{S} \underline{A} \underline{I} \underline{N} \underline{A} \underline{T} \underline{I} \underline{O} \underline{N} \Rightarrow \frac{10!}{3! \times 2! \times 2!}$$
$$\Rightarrow \underline{\underline{151200}} \text{ Ans}$$

Q2 → MATHEMATICS → arrange, all consonants together.

$$n = 11$$

Con → 7 (M=2, T=2)

Vow → 4 (A=2)



$$\frac{5! \times 7!}{2! \cdot 2! \cdot 2!} \Rightarrow \underline{\underline{75600}} \text{ Ans}$$

Q3 → UNIVERSITY

i) all vowels together

ii) all vowels not together.

i) $n=10, r=4 (i=2)$

u	i	i	e	x	x	n	s	t	y
7	6	5	4	3	2	1			

$$\frac{7! \times 4!}{2!} \Rightarrow 5040 \times 4 \times 3 \Rightarrow \underline{60480} \text{ Ans}$$

ii) $\frac{10!}{2!} = 1814400 \rightarrow \text{Total arrangement}$

Total - together

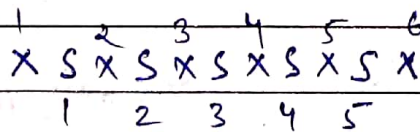
$$1814400 - 60480 \Rightarrow 1753920$$

Q1 $\rightarrow 7 \rightarrow$ students (total)

2 \rightarrow Math

5 \rightarrow other subject

In which manner they sit by which math student never sit together.



$$\begin{aligned} & 7! - (6! \times 2) \\ & 6! (7-2) \\ & 720 \times 5 = \underline{3600} \end{aligned}$$

$${}^6P_2 \times 5! \Rightarrow 6 \times 5 \times 120 \Rightarrow \underline{3600} \text{ Ans}$$

Q2 $\rightarrow 2, 3, 0, 3, 4, 2, 3$ | 10 lakh at 1st part
 $n=7$ | 2nd part at 2nd part

3's \rightarrow 3 time

2's \rightarrow 2 time

with 7 no. $\frac{7!}{3!2!}$

but no. never start with 0 then $n=6$

$\frac{6!}{3!2!}$

$\frac{7!}{3!2!} - \frac{6!}{3!2!} \Rightarrow \frac{6!}{3!2!} (7-1)$

$\frac{6 \times 5 \times 4}{2} \times 6 = 360$ Ans

Q1 \rightarrow 6 \rightarrow men sit on circular table but 2 female
3 \rightarrow female never sit together.

6 men circ. table $\rightarrow 6-1! \Rightarrow 5!$

${}^6P_3 \times 5! \Rightarrow 6 \times 5 \times 4 \times 120 \Rightarrow 14400$ Ans

Q2 \rightarrow 0, 1, 2, 3, 4, 5 five digit which divisible by 3.

1st \rightarrow 1, 0, 2, 4, 5

2nd \rightarrow 1, 2, 3, 4, 5

for 1st $\frac{4 \times 4 \times 3 \times 2 \times 1}{1} \Rightarrow 96$
for 2nd $\frac{5 \times 4 \times 3 \times 2 \times 1}{1} \Rightarrow 120$
 $96 + 120 = 216$ Ans

for 2nd $\frac{5 \times 4 \times 3 \times 2 \times 1}{1} \Rightarrow 120$

"Some Question on Permutation"

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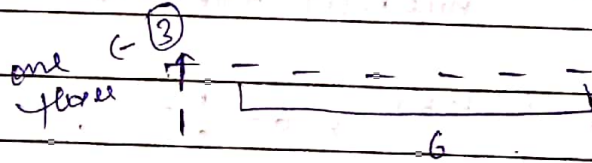
Q1 → How many words of 11 letters could be formed with all the vowels at even places, using all the letters of alphabet (not repetitions)

1 A 2 E 3 I 4 O 5 U 6
 1 2 3 4 5 6 7 8 9 10 11

total → 26-5
 → 21

$${}_{21}P_6 \times 5! \quad \underline{\underline{\text{Ans}}}$$

Q2 → How many 7-digit no. are there having the digit 3 three times & the digit 0 four times.



3 are → 3
 0 → 4

$$\frac{6!}{3! 4!} = 15 \quad \underline{\underline{\text{Ans}}}$$

Q3 → In how many ways can a person send invitation card to 6 of his friends if he has four servants to distribute the cards?

servant 4 → servant, 6 → friend

no. of way → 4^6
Ans